

The Huntington-Hill Method – Version 2

Lecture 25
Section 4.5

Robb T. Koether

Hampden-Sydney College

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- 1 Version 2
- 2 Examples
- 3 Version 1 or Version 2?
- 4 Assignment

Outline

1 Version 2

2 Examples

3 Version 1 or Version 2?

4 Assignment

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- Repeat the previous 2 steps until all the seats have been apportioned.
- Note that on each iteration only the q that was changed and its quotient need to be updated.**

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Example

Example (Example – Version 2)

- The populations of three states are 3, 7 and 10 million people, respectively.
- The total number of seats apportioned to those states is 7.
- Use Version 2 to determine how many seats each state should get.

Example

Example (Example – Version 2)

State	Population (p)	Seats (q)	$D = \sqrt{q(q+1)}$	p/D
A	3	1	$\sqrt{1 \cdot 2} = 1.41$	$\frac{3}{\sqrt{2}} = 2.12$
B	7	1	$\sqrt{1 \cdot 2} = 1.41$	$\frac{7}{\sqrt{2}} = 4.94$
C	10	1	$\sqrt{1 \cdot 2} = 1.41$	$\frac{10}{\sqrt{2}} = 7.07$

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C	10	4	$\sqrt{3 \cdot 4} = 3.46$	$\frac{10}{\sqrt{12}} = 2.88$

Example

Example (Example – Version 2)

- The populations of WY, VT, ND, RI, NH, and NE are 564, 626, 673, 1053, 1316, and 1826 thousand people, respectively.
- The total number of seats apportioned to those states is 10.
- Use Version 2 to determine how many seats each state should get.

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- Work this example with $M = 12$.

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- Chapter 4 Exercises 49, 50. Use Version 2 with $M = 10$.